# One-Bit Hard Combination Decision Scheme for Cooperative Spectrum Sensing in Cognitive Radio

Md. Shamim Hossain, Md. Ibrahim Abdullah, Mohammad Alamgir Hossain Computer Science and Engineering, Islamic University, Bangladesh

Article Info	ABSTRACT
Article history: Received Mar 16, 2015 Revised Jun 17, 2015 Accepted Jul 20, 2015	In this paper, the performance of 1-bit hard combination decision scheme for cooperative spectrum sensing in Cognitive Radio has been studied to maximize the probability of primary user detection. Energy detector model is used to observe the presence of primary user signal. Simulation result shows that the probability of missed detection is decreasing for both conventional and 1-bit hard combination OR rule with increasing the probability of false
<i>Keyword:</i>	alarm correspondingly. It also has demonstrated that 1-bit hard combination
Cne-bit hard combination	decision scheme exhibits comparable performance with the conventional
Cognitive radio	one-bit scheme and thus achieves a good tradeoff between performance and
Cooperative spectrum sensing	complexity.
Data fusion	Copyright © 2015 Institute of Advanced Engineering and Science.
Energy detection	All rights reserved.

## Corresponding Author:

Md. Shamim Hossain, Lecturer, Dept. of CSE, Islamic University, Bangladesh. Email: shamimmalitha@yahoo.com

# 1. INTRODUCTION

In In recent years, cognitive radio (CR) has emerged as a promising paradigm for exploiting the spectrum opportunity, which is restricted by the current rigid spectrum allocation scheme, to solve the spectrum scarcity problem [1]. One of the fundamental challenges in spectrum sensing is to reliably detect the primary users (PUs) signals. In CR terminology, primary user (PU) can be defined as the licensed user who has rights on the usage of a specific part of the spectrum. On the other hand, CR user sense the RF environment without causing interference to PUs, identify the available spectrum if PUs are absent and change its radio parameters to used the unoccupied spectrum. The fundamental task of CR users is to detect the presence of PUs through spectrum sensing. A number of different techniques have been proposed for identifying the presence of the PU. The existing spectrum sensing techniques can be broadly divided into three categories [2]: cyclostationary detection [2], matched filter detection [3] and energy detection [12]. Among them, energy detection has been widely applied since it does not require any a priori knowledge of the primary signals and has much lower complexity than the other two schemes. But spectrum sensing is a tough task because of shadowing, fading, and time-varying natures of wireless channels. To combat these impacts, cooperative spectrum sensing schemes have been proposed to obtain the spatial diversity in multiuser CR networks [4]-[10]. In cooperative spectrum sensing, information from different CR users is combined to make a decision on the presence or absence of the primary user. Cooperation among CR user is usually coordinated by a fusion center through hard or soft decision fusion strategies. In hard decision technique the individual CR user makes the one-bit decision regarding the existence of the PU. The bit-1 indicates the presence of PUs. After observing the PU signal, the local detection forwards them to data fusion centre for further process. The final decision then is taken by combining all local detection based on OR. In the case of soft decision, the decision is taken by correlating the measurement made by individual users in signal detection.Conventional one-bit hard decision for cooperative spectrum sensing has been investigated in [9-11] and one-bit weighted hard combination for cooperative spectrum sensing proposed in [15]. This

paper investigates the performance of 1-bit hard combination scheme for cooperative spectrum sensing in Cognitive Radio.

The rest of this letter is organized as follows. In section II describes system model of energy detection. One-bit Hard combination scheme with OR rule was discussed on section III. Section IV discusses the simulation result and finally conclusion is drawn in section V.

#### 2. SYSTEM MODEL

The energy detector consists of a square law device followed by a finite time integrator (fig.-1). The noise pre-filter serves to limit the noise bandwidth and to select the bandwidth of interest. The noise at the input to the squaring device has a band-limited, flat spectral density [12]. The output of the integrator at any time is the energy of the input to the squaring device over the interval T in the past.

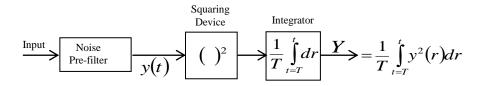


Figure 1. Energy Detection

Finally, this output signal Y is compared to the threshold in order to decide whether a signal is present or not. The threshold is set according to statistical properties of the output Y when only noise is present.

Consider a CR network with *N* cooperative users and *M* samples are utilized. The energy detection [12] [13] is applied at each CR user. The received signal at the *i*th sample of the *j*th CR user  $r_{ji}$ ,  $1 \le j \le N$ ,  $1 \le i \le M$ , is given by

$$r_{ji} = \begin{cases} n_{ji}, & H_0 \\ \sqrt{\gamma_j} s_{ji} + n_{ji}, & H_1 \end{cases}$$
(1)

where  $\sqrt{\gamma_j} s_{ji}$  denotes the received primary signal with the average power  $\gamma_j$  and  $n_{ji}$  denotes the white noise. In eq. 1,  $H_0$  and  $H_1$  denote the hypotheses corresponding to the absence and presence of the primary signal respectively. The goal of energy detection is to decide between the two hypotheses. The received signal  $r_{ii}$  is Gaussian with [14],

$$r_{ji} \approx \begin{cases} N(0,1), & H_0 \\ N(0,1+\gamma_j), & H_1 \end{cases}$$
<sup>(2)</sup>

According to eq. 2, the observed energy in at the *j*th CR user is given by [14]

$$Y_{j} = \sum_{i=1}^{M} r_{ji}^{2} = \begin{cases} b_{j0}, & H_{0}, \\ (1+\gamma_{j})b_{j1}, & H_{1}, \end{cases}$$
(3)

where random variables  $b_{j0}$  and  $b_{j1}$  follow a central chi-square distribution with *M* degrees of freedom. Let  $\lambda$  be the local decision threshold for each CR user, then the local false alarm probability  $P_f$  and detection probability  $P_f$  can be obtained from eq. 3 as,

$$P_{d} = \Pr(Y > \lambda \mid H_{1}) = Q_{u}(\sqrt{2\gamma}, \sqrt{\lambda})$$
<sup>(4)</sup>

$$P_{f} = \Pr(Y > \lambda \mid H_{0}) = \frac{\Gamma\left(u, \frac{\lambda}{2}\right)}{\Gamma(u)}$$
(5)

where  $\Gamma(\cdot)$ ,  $\Gamma(\cdot, \cdot)$ ,  $\gamma$  and  $Q_u$  denote the gamma function, upper incomplete gamma function, signal to noise ratio (SNR) and generalized Marcum's Q function respectively.

## 3. ONE-BIT HARD COMBINATION SCHEME

In the conventional one-bit hard combination scheme, there is only one threshold dividing the whole range of the observed energy into two regions. As a result, all of the CR users above this threshold are allocated the same weight regardless of the possible significant differences in their observed energies. Intuitively, a better detection performance can be achieved if we divide the whole range of the observed energy into more regions, and allocate larger weights to the upper regions and smaller weights to the lower regions. Based on the above heuristic, 1-bit hard combination scheme which we describe below.

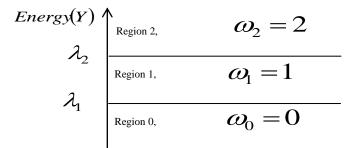


Figure 2. Principle Of 1-Bit Hard Combination Scheme

Fig. 2 shows the principle of 1-bit hard combination scheme. Different from the conventional onebit scheme with only one threshold, two thresholds [15] in 1-bit scheme  $\lambda_1$  and  $\lambda_2$  are adopted to divide the whole range of the decision statistic of the local spectrum sensing into three regions. In the fusion center, if the energy value falls into the corresponding region, it will be judged as "1", no information or "0". This decision criterion is equivalent to allocating the 3 regions different weights  $\omega_0 = 0$ ,  $\omega_1 = 0$ ,  $\omega_2 = 0$  and the weighted summation is given by

$$N_c = N_2 \cdot \omega_2 + N_1 \cdot \omega_1 \tag{6}$$

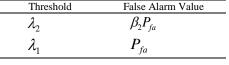
where  $N_1$  is the number of local detectors the energies of which are greater than  $\lambda_1$  and less than  $\lambda_2$ ,  $N_2$  is the number of local detectors the energies of which are greater than  $\lambda_2$ . The decision rule [15] adopted is given by

$$D = \begin{cases} 1 & N_c \ge 1 \\ 0 & otherwis \end{cases}$$
(7)

Each CR user needs to feedback one bit information to indicate which region its observed energy falls in. The primary signal will be declared present if any one of the observed energies falls in region 2, or one of them fall in region 1. In this criterion, while determining the threshold, probability of false alarm  $P_{fa}$  is fixed to some value and the probability of detection  $P_d$  is maximized. Table 1 shows the  $P_{fa}$  values chosen for determining the two thresholds.

69

Table 1. Threshold and the corresponding false alarm values in the 1-bit hard combination scheme



The coefficients  $\beta_n$  in Table 1 are found by

$$\beta_n = (n-1) \times 10^{-(n-1)}, n=2$$
 (8)

where *n* is the threshold index and  $\beta_1 = 1$ .

For the 1-bit hard combination scheme, thresholds  $\lambda_1$  and  $\lambda_2$  need to be determined to meet the target overall false alarm probability of the *N*-user CR network  $Q_F$  exactly, and also to optimize the detection performance.

Table 2. Energy regions and corresponding weights in the 1-bit hard combination scheme

Region	Weight
2	$w_2 = 2$
1	$w_1 = 1$
0	$w_0 = 0$

Weights shown in Table 2 are determined in the following manner. If 50% of all CR users observe energy in Region 2, with no observed energies in other regions, or 100% of all Cognitive Radio Users observe energy in Region 1 with no observed energies in other regions, the signal of interest is said to be present. Table 2 summarizes the percentage of CR users required in a given region to declare the presence of the signal of interest, with no observed energies in other regions. While other percentage values are possible, the chosen values in Table 3 provided satisfactory results.

Table 3. Design for determ	nining the weights of the 1-bit hard combination scheme
Region	Required number of Cognitive Users to
	declare the presence of signal of interest in a
	given region with no observed energies in

	given region with no observed energies in other regions
2	50% of all Cognitive Users
1	100% of all Cognitive Users
0	-

Let  $Q_{f^2}$  be the probability that one or more observation local energy values are greater than  $\lambda_2$  and  $Q_{f^1}$  be the probability that more than  $N_1 = \lfloor 1/\omega_1 \rfloor$  observation local energy values are greater than  $\lambda_1$  and less than  $\lambda_2$ . We have [15]

$$Q_{f2} = 1 - P(N_2 = 0 \mid H_0) = 1 - (1 - P_{f2})^N$$
(9)

$$Q_{f1} = P(N_2 = 0 | H_0) \cdot \sum_{J=N_1}^{N} P(N_1 = j | H_0)$$
  
=  $(1 - P_{f2})^N \cdot \sum_{j=N_1}^{N} {N \choose j} (P_{f1} - P_{f2})^j \cdot (1 - P_{f1} + P_{f2})^{N-j}$  (10)

One-Bit Hard Hard Combination Decision Scheme for .... (Md. Shamim Hossain)

where  $P_{fn}$  is the probability that the local energy value is greater than  $\lambda_n$  and according to (5)

$$P_{fn} = P(S_0 > \lambda_n) = \frac{\Gamma\left(\frac{M}{2}, \frac{\lambda_n}{2}\right)}{\frac{M}{2}}$$
(11)

$$\lambda_n = 2\Gamma^{-1}\left(\frac{M}{2}, P_{fn}\Gamma\left(\frac{M}{2}\right)\right) \tag{12}$$

 $\Gamma^{-1}(\cdot,\cdot)$  denotes the inverse of the incomplete gamma function. Then the probability of false alarm in the fusion center can be expressed as

$$Q_f = Q_{f1} + Q_{f2} \tag{13}$$

Suppose all the channels between the primary user and secondary users are independent identically distributed. The probability of detection [15] in the fusion center can be expressed

$$Q_{d} = 1 - (1 - P_{d2})^{N} + (1 - P_{d2})^{N} \cdot \sum_{j=N_{1}}^{N} {N \choose j} (P_{d1} - P_{d2})^{j} \cdot (1 - P_{d1} + P_{d2})^{N-j}$$
(14)

where  $P_{dn}$  is the probability that the local energy value is greater than  $\lambda_n$ .

# 4. SIMULATION RESULT

All simulation was done on MATLAB version R2011a under AWGN channel by taking time bandwidth factor u=1000 and the probability of false alarm is used from 0.01 to 1. The number of samples adopted are M=2000. "OR" rule is employed for 1-bit hard combination scheme.

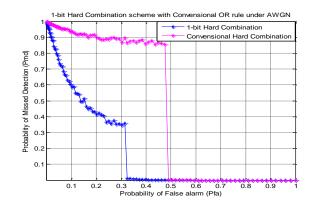


Figure 3. ROC of conventional and 1-bit OR rule with 10 CR users

Figure 3 shows complementary ROC of conventional OR rule and 1-bit OR rule in the hard combination scheme. Where 10 CR users and SNR=15dB were taken. Simulation result shows that probability of missed detection in 1-bit hard combination scheme is reduced significantly than the

conventional hard combination scheme although same CR user is used. 1-bit hard combination scheme has much better performance than the conventional one-bit scheme.

Figure 4 shows complementary ROC of 1-bit hard combination scheme. Where 10 CR users and SNR=5dB, 10dB, 15dB and 20dB were taken. Simulation result shows that the probability of missed detection is decreased when SNR is increased. It also shows that the probability of missed detection is decreasing significantly by changing the SNR. So SNR influences on the detection probability.

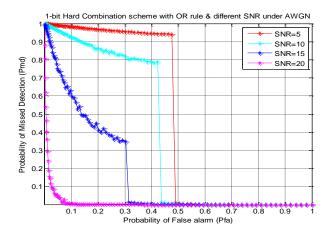


Figure 4 ROC of 1-bit OR rule with 10 CR users & different SNR

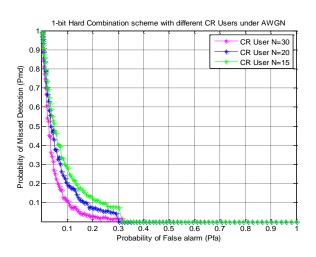


Figure 5. ROC of 1-bit OR rule with different CR users

Figure 5 shows complementary ROC of 1-bit hard combination scheme. Where SNR =15dB and CR user N=15, 20 and 30 were taken in this simulation. Simulation result shows that probability of missed is decreased when CR user is increased. So, 1-bit hard combination scheme for cooperative spectrum sensing in CR maximize the detection probability.

### 5. CONCLUSION

In this paper, the performance of 1-bit hard combination decision scheme for cooperative spectrum sensing in Cognitive Radio has been studied. Simulation result demonstrated that the probability of missed detection is decreasing for both conventional hard combination and 1-bit hard combination scheme with OR rule correspondingly with increasing the probability of false alarm. It is shown that 1-bit scheme has much better performance than the conventional one-bit hard combination scheme. The probability of missed

detection is decreased even though CR user is increased. The 1-bit hard combination scheme exhibits much better performance than the conventional one-bit scheme.

## REFERENCES

- [1] S. Haykin, "Cognitive Radio: Brain-Empowered Wireless Communications," *IEEE J. Selected Areas in Communications*, vol. 23, no. 2, Feb. 2005, pp. 201-220.
- [2] D. Cabric, S. M. Mishra, and R. W. Brodersen, "Implementation Issues In Spectrum Sensing For Cognitive Radios," in *Proc. Asilomar Conf. on Signals, Systems, and Computers*, Nov. 2004, vol. 1, pp. 772–776.
- [3] H. Tang, "Some Physical Layer Issues of Wide-Band Cognitive Radio Systems," *IEEE Int. Conf. Wireless Networks, Commun and Mobile Computing*, pp.151-159, Nov.2005.
- [4] G. Ganesan and Y. (G.) Li, "Cooperative spectrum sensing in cognitive radio-part I: two user networks", *IEEE Trans. Wireless Commun*, vol.6, no.6, pp. 2204–2213, June 2007.
- [5] G. Ganesan and Y. (G.) Li, "Cooperative spectrum sensing in cognitive radio part II: multiuser networks," *IEEE Trans. Wireless Comm.*, vol. 6, no. 6, pp. 2214–2222, Jun 2007.
- [6] A. Ghasemi and E. S. Sousa, "Collaborative spectrum sensing for opportunistic access in fading environments," in *Proc. IEEE Int. Symp on New Frontiers in Dynamic Spectrum Access Networks*, Nov. 2005, pp. 131–136.
- [7] S. M. Mishra, A. Sahai, and R. W. Brodersen, "Cooperative sensing among cognitive radios," in *Proc. IEEE Int. Conf. on Commun.*, June 2006, vol. 4, pp. 1658–1663.
- [8] Ghasemi A, Sousa E S, "Collaborative Spectrum Sensing for Opportunistic Access in Fading Environments", Proceedings of DySPAN 2005. Baltimore, *Maryland USA: IEEE Press*, 2005: 131–136.
- [9] Renzor M Di, Graziosi F, Sanyucci CI F, "Cooperative Spectrum Sensing in Cognitive Radio Networks over Correlated Log-Normal Shadowing", Proceedings of VTC 2009-Spring. Barcelona, Spain: IEEE Press, 2009:1–5.
- [10] Mishra S M, Sahai A, Brodersen Rw, "Cooperative Sensing among Cognitive Radios", Proceedings of ICC'06. Istanbul, *Turkey: IEEE Press*, 2006: 1658–1663.
- [11] N. Armi, N.M. Saad & M. Arshad, "Hard Decision Fusion based Cooperative Spectrum Sensing in Cognitive Radio System", ITB J. ICT Vol. 3, No. 2, pp.109-122, 2009.
- [12] H. Urkowitz, "Energy detection of unknown deterministic signals," Proc. IEEE, vol. 55, pp. 523-531, Apr. 1967.
- [13] F. F. Digham, M. -S. Alouini, and M. K. Simon, "On the energy detection of unknown signals over fading channels," in Proc. IEEE Int. Conf. on Commun. May 2003, vol. 5, pp. 3575–3579.
- [14] Ma, G. Zhao, and Y. Li, "Soft combination and detection for cooperative spectrum sensing in cognitive radio networks," *IEEE Trans. Wireless. Commun.* vol. 7, no. 11, pp. 4502–4507, Nov. 2008.
- [15] Li Jiajun, Tan Zhenhui, Ai Bo and Yang Shan, "Weighted Hard Combination for Cooperative Spectrum Sensing in Cognitive Radio Networks", *Research paper*, pp. 111-116, 2011.

# **BIOGRAPHIES OF AUTHORS**



**Md. Shamim Hossain** has been received Bachelor's and Master's degree in computer science and engineering from Islamic University, Kushtia-7003, Bagladesh. Courrently he is a Lecturer of the Department of CSE, Islamic University, Kushtia. His areas of interest include wireless communication, WSN & Cognitive Radio. His work has produced 10 peer-reviewed scientific International Journal papers.



**Md. Ibrahim Abdullah** has been received the Bachelor's, Master's and M.Phil degree in Applied Physics & Electronics from Rajshahi University, Rajshahi. Courrently he is as Associate Professor of the department of CSE, Islamic University, Kushtia-7003, Bangladesh. His areas of interest include Network security, Wireless Sensor Network, mobile communication & Cognitive Radio.



**Mohammad Alamgir Hossain** received his B.SC degree with honors in Computer Science and Engineering (CSE) from Islamic University (IU), Kushtia-7003, Bangladesh, in 2010 and his M.SC degree in same department, in 2012. His current research interest is in the area of OFDM and Cognitive Radio.